

Unit 7 Class Work

### Solving Exponential Equations Class Work

Objective: You will be able to solve exponential equations. (only practice)

**\* Equivalence of Exponents**

Example 1: Solve for x.  
 $11^{3x} = 11^{5x+12}$   
 If the bases are the same, the exponents are equal.  
 $3x = 5x + 12$   
 $-2x = 12 \Rightarrow x = -6$

Example 2: Solve for x.  
 $(3^x)^4 = (3^2)^{3x-8}$  \*rewrite w/ common base 1st  
 $2(x-4) = 3(3x-8)$  \*set exponents  
 $2x-8 = 9x-24$   
 $-7x = -16 \Rightarrow x = 16/7$

**Practice:** Solve for the variable in each equation.

1.  $4^{2w} = 16^{w-18}$   
 $2w = 2w - 18$   
 $-4w = -18$   
 $w = 9/2$

2.  $15^{x+2} = 15^{3x+10}$   
 $x+2 = 3(-x+12)$   
 $x+2 = -3x+36$   
 $4x = 34$   
 $x = 34/4 = 17/2$

3.  $8^r = 1/2^{2r-4}$   
 $(2^3)^r = (2^{-1})^{2r-4}$   
 $3r = -2r + 4$   
 $5r = 4$   
 $r = 4/5$

4.  $5^{s-1} = 25^{s-3}$   
 $5^{s-1} = 5^{2(s-3)}$   
 $s-1 = 2s-6$   
 $-s = -5$   
 $s = 5$

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HW

Solve each equation.

1.  $93^{3x+2} = 93^{-4(x+5)}$

2.  $36^{5x-1} = \left(\frac{1}{216}\right)^{3x}$

3.  $343^{2x+7} = 49^{-4x-9}$

4.  $32^{-(5x+3)} = \left(\frac{1}{2}\right)^8$

Solutions

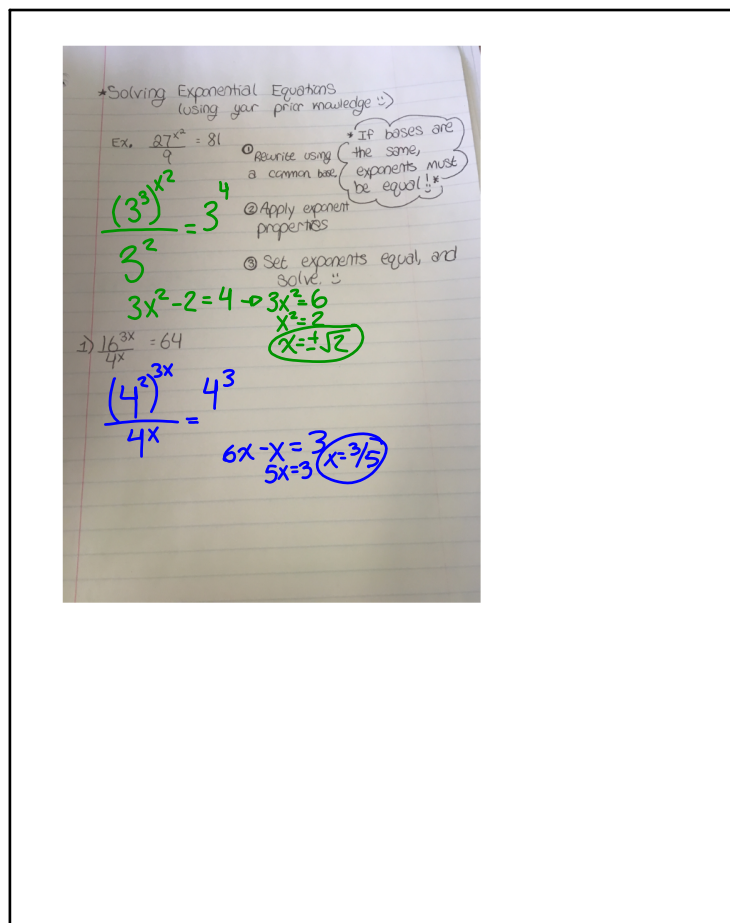
1.  $-22/7$

2.  $2/19$

3.  $-39/14$

4.  $-7/25$

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2)  $3 \cdot 2^{2x+1} \cdot 16^{2x-4}$

$$(2^3)^{2x+1} \cdot (2^4)^{2x} = 2^2$$

$$10x + 5 + 8x = 2$$

$$18x = -3$$

$$x = -\frac{3}{18} \quad x = -\frac{1}{6}$$

3)  $27^{x-1} \cdot 81^{5x} = 9$

$$(3^3)^{x-1} \cdot (3^4)^{5x} = 3^2$$

$$3x - 3 + 20x = 2$$

$$23x = 5 \quad x = \frac{5}{23}$$

4)  $\frac{125^{2x}}{25^x} = 625$

$$x = 1$$

5)  $7^{3x-1} \cdot 343^{5x} = 49^{2x+1}$

$$7^{3x-1} \cdot (7^3)^{5x} = (7^2)^{2x+1}$$

$$3x - 1 + 15x = 4x + 2$$

$$x = \frac{3}{14}$$

6)  $\frac{1}{81^x} \cdot \frac{1}{3} = 9^{5x+1}$

$$(3^{-4})^x \cdot 3^{-1} = (3^2)^{5x+1}$$

$$-4x - 1 = 10x + 2$$

$$-14x = 3 \quad (x = -3/14)$$

7)  $\frac{64^{2x+3}}{(32^{5x})} = 8^{3x}$

$$\frac{(2^6)^{2x+3}}{(2^5)^{5x}} = (2^3)^{3x}$$

$$12x + 18 + 25x = 9x$$

$$37x = 9x - 18$$

$$28x = -18$$

$$x = -18/28 = -9/14$$

Algebra 2 Name: \_\_\_\_\_

Solving Exponential Equations Using Prior Knowledge

Solve each equation.

1)  $16^{2x-1} = 64$                       2)  $\frac{125^x}{625^{2x}} = \frac{1}{625}$

3)  $\left(\frac{1}{4}\right)^{2x-3} = 64 = 16$                       4)  $36^{2x-1} \cdot 216^{3x-10} = 36$

5)  $8^{-2x} \cdot 32^{2x-1} = 64$                       6)  $216^{2x} \cdot \frac{1}{36} = 1$

7)  $\frac{9^{-2x}}{27^{2x}} = 9^{2x-1}$                       8)  $\frac{343^{2x}}{49^{2x}} = 49^{-2x}$

\*what if you had  $4^{x+2} = 7^{3x-7}$  ... we will learn soon!\*