

1 Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = x$

Find:  $h(x) = (f - g)(x)$

$$3x^2 + 2x + 1$$

$$4x^2 + 2x$$

$$3x^2 + 3x$$

$$\underline{3x^2 + x}$$

$$(3x^2 + 2x) - x$$

Answer

Operations with Functions

2 Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = x$

Find:  $h(x) = \left(\frac{f}{g}\right)(x)$

$$3x + 2x$$

$$\underline{3x + 2}$$

$$\underline{3x^2 + 2x}$$

$$\underline{2}$$

$$\underline{\underline{1}}$$

$$3x + 2$$

$$3x \cancel{x}$$

$$\cancel{3x^2 + 2x} \cancel{x}$$

Answer

Operations with Functions

3.

### Combined Functions

You may also be asked to evaluate combined functions when given specific values for x.

Given  $f(x) = (x - 8)^2$  &  $g(x) = x^3$ , find:

Answer

$$(f * g)(5)$$

*every  
replace "x" with 5*

*input  
is a → output  
is a*

$f(5) = (5 - 8)^2 = \underline{\underline{9}}$

$g(5) = 5^3 = \underline{\underline{125}}$

$(f * g)(5) = 9 \cdot 125$   
 $= \underline{\underline{1125}}$

Operations with Functions

4.

If  $f(x) = 2x + 1$  &  $g(x) = x^2$ , create

Answer

$$h(x) = f(3x) \bullet g(2x)$$

$$(2(3x)+1) \bullet (2x)^2$$

$$(6x+1) \bullet 4x^2$$

$$\underline{\underline{24x^3 + 4x^2}}$$

Operations with Functions

5. If  $f(x) = 5x$  &  $g(x) = \frac{1}{4x}$ , which equation represents  $h(x) = \frac{g(-x)}{f(2x)}$  ?

$$h(x) = -\frac{5x}{2}$$

$$h(x) = -\frac{2x}{5x}$$

$$h(x) = \frac{1}{40x^2}$$

$$h(x) = -\frac{1}{40x^2}$$

Answer

Operations with Functions

6. If  $f(x) = 3x + 2$  &  $g(x) = -2x + 3$ , which equation represents  $h(x) = -2f(2x) - 3g(3x)$ ?

$$h(x) = -6x + 35$$

$$h(x) = 6x - 35$$

$$h(x) = 6x - 13$$

$$h(x) = -6x + 13$$

Answer

Operations with Functions

7. If  $f(x) = -2x$  &  $g(x) = 4x$ , create  $h(x) = \frac{f(2x)}{3g(x)}$ .  
Is this equivalent to  $\frac{x}{3}$ ?

Answer

Operations with Functions

8. If  $f(x) = x^2 + 2$  &  $g(x) = -x + 1$ , create  
 $h(x) = 2g(-x) - f(2x)$ . Is this equivalent to  
 $-4x^2 + 2x + 4$ ?

Answer

Operations with Functions

9. The functions  $f$  and  $g$  are defined by  
 $f(x) = x^2$  &  $g(x) = 2x$ , respectively. Rewrite the function  
 $h(x) = \frac{f(2x)g(-2x)}{2}$  in terms of  $x$ .

$h(x) = -4x^3$

$h(x) = -8x^3$

$h(x) = -2x^3$

$h(x) = 8x^3$

Answer

PARCC Sample Q

10. Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = x$

Find:  $h(x) = 2f(x) - xg(x)$

$6x^2 + 3x$

$4x^2 + 2x$

$6x^2 + x$

$5x^2 + 4x$

$f(x) = 3x^2 + 2x$  multiply all terms by 2  
 $2f(x) = \underline{\underline{6x^2 + 4x}}$

$g(x) = x$

$x \cdot g(x) = x \cdot x = \underline{\underline{x^2}}$

$\underline{\underline{6x^2 + 4x - x^2}}$

Answer

$$\textcircled{12} \quad \left( \frac{3N}{2M} \right)(0)$$

$$N(x) = -3x + 4$$

$$M(x) = 9x^3 - 1$$

• replace

$$x \text{ with } 0$$

$$N(0) = -3(0) + 4 = 4$$

$$M(0) = 9(0)^3 - 1 = -1$$

$$\frac{3(4)}{2(-1)} = \frac{12}{-2} = \boxed{-6}$$

Oct 10-8:31 AM

Oct 8-12:49 PM

# Composite Functions

**Composite functions** exist when one function is "nested" in the other function.

There are 2 ways of writing a composite function:

$$f(g(x)) \text{ or } f \circ g(x)$$

Each form is read "f of g of x" and both mean the same thing.

Composite Functions

# Composite Functions

To simplify composite functions, substitute one function into the other in place of "x" and simplify. Work from the inside out.

Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = 4x$

Find:  $f(g(x))$

Answer

Composite Functions

## Composite Functions

To simplify composite functions, substitute one function into the other in place of "x" and simplify. Work from the inside out.

2.

Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = 4x$

Find:  $g(f(x))$

Answer

Composite Functions

## Composite Functions

3.

Given:  $f(x) = x - 3$  &  $g(x) = 2x^2 + x - 2$

Find:  $f(g(x))$

Answer

Composite Functions

## Composite Functions

4. Given:  $f(x) = x - 3$  &  $g(x) = 2x^2 + x - 2$

Find:  $g \circ f(x)$

Answer

Composite Functions

5. Find  $f \circ g(x)$  if  $f(x) = x^2 + x + 4$  &  $g(x) = \sqrt{x}$

$$x + \sqrt{x + 4}$$

$$\sqrt{x^2 + x + 2}$$

$$x + \sqrt{x} + 2$$

$$x + \sqrt{x + 4}$$

Answer

Composite Functions

6. Find  $f \circ g(x)$  if  $f(x) = x^2$  &  $g(x) = \sqrt{x^2 + 4}$

$$x^2 + 4$$

$$x^2 + 2$$

$$\sqrt{x^4 + 4}$$

$$\sqrt{6x}$$

Answer

Composite Functions

## Composite Functions

To simplify composite functions with numerical values, there are two different options:

- 1) substitute the number into the "inner" function, simplify, and then substitute that value in for the variable in the "outer" function.
- 2) find your composite function & then substitute the numerical value into the composite function.

If  $f(x) = x^2 - 4x$  &  $g(x) = 3x + 2$ , then find  $f(g(1))$ .

Option 1)

$$\begin{aligned}g(1) &= 3(1) + 2 = 5 \\f(g(1)) &= f(5) \\&= 5^2 - 4(5) \\&= 25 - 20 = 5\end{aligned}$$

Option 2)

$$\begin{aligned}f(g(x)) &= (3x + 2)^2 - 4(3x + 2) \\&= 9x^2 + 12x + 4 - 12x - 8 \\&= 9x^2 - 4 \\f(g(1)) &= 9(1)^2 - 4 = 5\end{aligned}$$

Composite Functions

## Composite Functions

7. Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = 4x$

Find:  $f \circ g(3)$

Answer

Composite Functions

## Composite Functions

8. Given:  $f(x) = 3x^2 + 2x$  &  $g(x) = 4x$

Find:  $g(f(-2))$

Answer

Composite Functions

9. If  $f(x) = x^2 + 1$  &  $g(x) = 3x - 1$ , find the value of  $f(g(2))$

Answer

Composite Functions

10. If  $f(x) = x + 2$  &  $g(x) = \frac{1}{x}$ , find the value of  $g(f(-2))$

Answer

$$\begin{array}{l} \frac{5}{2} \\ \frac{1}{2} \end{array}$$

Composite Functions

11. If  $f(x) = 3x^2 + 2x - 3$  &  $g(x) = x - 2$ , find the value of  $f(g(-3))$

Answer

Composite Functions

Challenge: If  $f(x) = x + 1$ ,  $g(x) = 3x - 1$  &  $h(x) = |x|$ , find the value of  $f \circ h \circ g(0)$

Answer

Composite Functions



Sep 22-6:55 PM